

On the zero set of super-Brownian motion

Abstract

We study the density of one-dimensional super-Brownian motion given by the non-negative solution of

$$\frac{\partial X(t, x)}{\partial t} = \frac{1}{2} \frac{\partial^2 X(t, x)}{\partial x^2} + \sqrt{X(t, x)} \dot{W}(t, x).$$

Here \dot{W} is a space-time Gaussian white noise. We determine the Hausdorff dimension of the boundary of the zero set of $X(t, \cdot)$. This is a joint work with C. Mueller and E. Perkins.